

SARDAR PATEL UNIVERSITY
M. Sc. Information Technology
 Semester – I External ATKT Examinations
PS01CINT03 – Introduction to Theoretical Computer Science
 7th April 2016, Thursday

Time: 10:30 a.m. to 01:30 p.m.

Max Marks: 70

Q-1 Choose the most appropriate option for each question.**[8]**

1. $X + X' = 1$ is _____.
 (A) Idempotent Law (C) Complement Law
 (B) Identity Law (D) Involution Law
2. Maximum number of edges in simple graph is _____.
 (A) $n(n-1)/2$ (B) $n-2$ (C) $n/n-2$ (D) None of these
3. _____ is used to denote the universal lower bound and _____ is used to denote universal upper bound.
 (A) 0, 0 (B) 1, 0 (C) 1, 1 (D) 0, 1
4. Replacing meet operation over join and join over meet operation is known as _____.
 (A) Principle of membership (C) Principle of lattices
 (B) Principle of duality (D) None of these
5. The Cardinality of a set A is denoted by notation like _____.
 (A) {A} (B) [A] (C) <A> (D) |A|
6. According to modus tollens if $P \Rightarrow Q$ and $\sim Q$ is true then _____ is true.
 (A) $\sim P$ (B) P (C) Q (D) $\sim P \vee Q$
7. A phrase structure grammar with no restriction is referred as _____ grammar.
 (A) type – 0 (B) type – 1 (C) type – 3 (D) None of these
8. _____ reflects the dynamic pace of movements of a phenomenon over a period of time.
 (A) Time series (C) Statistics
 (B) Frequency distribution (D) None of these

Q-2 Answer the following questions (Any Seven):**[14]**

- Define with and example: Lattice, Complete Lattice.
- Explain Weighted graphs and multigraphs.
- Draw Hasse diagram for the $\langle S60, D \rangle$ POSET.
- Draw a Truth table for $(P \wedge Q) \vee (P \wedge R)$.
- Explain utilities of time series with example.
- Define Algorithm.
- List the components of time series.
- Construct a grammar for the language $L = \{a^i b^{2i} / i \geq 1\}$.
- List the major components of phase structure grammar.

Q-3 Answer the following questions:

- Explain properties of binary relations with suitable example.
- Write a note on Injective and Bijective Functions.

[6]**[6]****OR**

- Write the shortest path algorithm.

[6]**Q-4 Answer the following questions:**

- Discuss tractable and intractable problems in detail. Also specify what is class of NP problem?
- Explain the use of lattices in design and implementation of digital networks in detail by taking appropriate example.

[6]**[6]****OR**

- Discuss Boolean Lattices and Boolean Algebra in detail with example.

[6]**Q-5 Answer the following questions:**

Fit a Straight line trend for the following series. Estimate the value for 2015.

a.	Year	2004	2005	2006	2007	2008	2009	2010
	Earnings (Rs. Lakhs)	60	72	75	65	80	85	95

[6]

- Write a De Morgan's Law and Prove them using truth table.

[6]**OR**

Determine trend of the following data using Semi-Average method and estimate the value for 2017.

b.	Year	2010	2011	2012	2013	2014	2015
	Profit	20	24	22	30	28	32

[6]**Q-6 Answer the following questions:**

- Write a note on fuzzy logic. Also explain fuzzy sets in brief.
- Given R and S are relation defined over sets $\{1,3,5\} \times \{1,3,5\}$ such that $R = \{(x,y) \mid y = x+2\}$ and $S = \{(x,y) \mid x < y\}$. Find Max-min composition $R \circ S$.

[6]**[6]****OR**

Let fuzzy set $\tilde{A} = \{(x_1, 0.3)(x_2, 0.8)(x_3, 1)\}$ and $\tilde{B} = \{(x_1, 0.4)(x_2, 0.1)(x_3, 0)\}$ be two fuzzy sets defined on universe of discourse X. Perform the following operations:

- (1) Find $\tilde{A} \cup \tilde{B}$ (2) Find $\tilde{A} \cap \tilde{B}$ (3) Find \tilde{A}^c

[6]**END****(2)**