[21 & A-11] Seat No. __

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SARDAR PATEL UNIVERSITY B. Sc. (I Semester) Examination 2016 Tuesday, 15th November 10.00 am - 12.00 pm US01CMTH01 - Mathematics Analytical Geometry & Complex Numbers

Note: Figures to the right indicates full marks of question	
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	10)
(1) Asymptotes of $y = \frac{x^2 - 1}{x^2 - 4}$ are	
(a) $x = 2$, -2 ; $y = 1$ (b) $x = 1$, -1 ; $y = 1$ (c) $x = 2$, -2 ; $y = 0$ (d) $x = 1$, -1 ; $\sqrt[4]{x} - 2$.	
(2) $y = \frac{2}{3x}$ is symmetric about	
(a) x-axis (b) y - axis (c) origin (d) none of these .	
(3) The shape of lemniscates looks, like	
(a) 8 (b) flower (c) rose (d) heart shape . (4) The curve of $r = \sin 4\theta$ is symmetric about	-
(a) polar axis (b) normal axis (c) pole (d) polar axis , normal axis and pole .	
(5) Polar equation of vertical line left to the pole is	
(a) $p = r \cos \theta$ (b) $p = r \sin \theta$ (c) $p = -r \sin \theta$ (d) $p = -r \cos \theta$.	
(6) If eccentricity $e < 1$ then conic is	
(a) hyperbola (b) parabola (c) circle (d) ellipse .	
(7) Centre of the circle $r = -9\sin\theta$ is	
(a) $(3, 3\pi/2)$ (b) $(9/2, 3\pi/2)$ (c) $(9/2, \pi/2)$ (d) $(9, 3\pi/2)$.	
(8) Amplitude of $-\sqrt{3} + i$ is	
(a) 60° (b) 150° (c) 30° (d) 120° .	
(9) Cube roots of unity are	
(a) 1,-1 (b) 1, $-\frac{1}{2} \pm i \frac{\sqrt{3}}{2}$ (c) 1, $\pm \frac{1}{2} \pm i \frac{\sqrt{3}}{2}$ (d) 1, $\frac{1}{2} \pm i \frac{\sqrt{3}}{2}$.	
(10) The value of $z + \frac{1}{z} = \dots$	

(c) $2sin\theta$

(a) $2\cos\theta$ (b) $\cos 2\theta$

Q-2 Answer any ten of the following:	
 (1) Find the parametric equation of √x + √y = √a. (2) Discuss symmetries of the curve y = x³/x²-1. (3) Transfer the equation in cartesian form: r = tanθ secθ. (4) Express the point (-√3, 1) in polar form. (5) Identify the curve 3(1 + cosθ). (6) find the radius and center of a circle r = 5cosθ. (7) find the polar equation of conic if directrix passes through a point (5, π/2) and 2/3. (8) Find polar equation of circle centre at (5, 225°) and radius is 2. (9) Find x-intercept and y-itercept of a curve y = 2/x²-x-2. (10) Find the real and imaginary part of z = (1 + 2i)(1 - 3i) (11) simplify (cosθ - isinθ)ⁿ (12) If z = x + iy the find z+z²/2 	(20) ;
Q-3(a) If a curve is given by $x = f(t)$; $y = g(t)$ and that both x and y get numerically lar as t approaches some number, say a. Then prove that oblique asymptote to the cur if it exist, is given by $y = mx + c$, where $m = \lim_{t \to a} \frac{dy}{dx} \text{ and } c = \lim_{t \to a} (y - mx).$	ge ve
Q-3(b) Sketch the curve given by $\frac{1}{2}$	[5]
Q-3(b) Sketch the curve given by $y = x^3 - 3x^2 + 2x$.	[5]
OR	
Q-3(a) Obtain the parametric equation of cycloid.	
Q-3(b) Find the asymptotes for the given curve by $r = t + \frac{1}{2}$ and $t = 1$	[5]
Q-4(a) State when a polar curve is symmetric with respect to normal axis? Prove it. Q-4(b) Sketch the curve $z=2$	[5]
Q-4(b) Sketch the curve $r = 2 + \cos\theta$.	[5]
	[5]
OR	
Q-4(a) State when a polar curve is symmetric with respect to polar axis? Prove it.	
$t = -16sin2\theta$	[5]
Q-5(a) In usual notation prove that the polar equation of conic is, $r = \frac{p e}{1 \pm e \cos \theta}.$	[5]
Q-5(b) Define: Reciprocal curve	[5]
Identify curve $r = 1 + 2\cos\theta$ also find its reciprocal curve sketch both of the curve with the same frame of reference.	[5]
OR	•
Q-5(a) Prove that polar equation of circle with centre (r_1, θ_1) and radius a is given by $r^2 + r_1^2 - 2rr_1cos(\theta - \theta_1) = a^2$. Also find equation of circle if center is on polar axis.	· [5]
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Q-5(b) In usual notation prove that polar equation of line is $p=rcos(\theta-\omega)$. Hence obtain equation of line

(i) perpendicular to polar axis (ii)parallel to polar axis.

[5]

Q-6(a) Prove that $(1 + \cos\theta + i\sin\theta)^n + (1 + \cos\theta - i\sin\theta)^n = 2^{n+1}\cos^n(\theta/2)\cos(n\theta/2)$.

[5]

Q-6(b) Solve $x^4 - x^3 + x^2 - x + 1 = 0$ by using De Moiver's theorem.

[5]

\mathbf{OR}

Q-6(a) State and prove De-Moiver's theorem.

[5]

Q-6(b) Expand $\cos^8\theta$ in a series of cosines.

[5]



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