(10)

Note : (1) Figures to the right indicate full marks.
(2) Log table and graph paper will be provided on request.

## Q. 1

(a) Derive mathematical form of a general linear programming problem.
(b) Solve the following linear programming problem by using simplex method.

$$
\text { Maximise } \quad Z=3 X_{1}+2 X_{2}
$$

$$
\text { Subject to } 2 x_{1}+X_{2} \leq 10
$$

$$
x_{1}+3 x_{2} \leq 6
$$

$$
x_{1}, x_{2} \geq 0
$$

(c) Solve the following linear programming problem by using graphical method. 05
Minimise $Z=x+y$

Subject to $\quad 5 x+10 y \leq 50$
$x+y \geq 2$
$y \leq 4$
$x, y \geq 0$

## OR

Q. 1
(a) Define following terms:

I Feasible solution.
II Constraints.
III Objective function.
IV Slack variable.
(b) Solve the following linear programming problem by using graphicai method.

Maximise $\quad Z=5 x+7 y$
Subject to $\quad 4 x+5 y \leq 200$ $3 x+5 y \leq 180$
$x, y \geq 0$
(c) Solve the following linear programming problem by using simplex method. 06 Maximise $\quad Z=5 X_{1}+7 X_{2}$
Subject to $\quad 4 X_{1}+5 X_{2} \leq 200$

$$
3 X_{1}+5 X_{2} \leq 180
$$

$$
2 x_{1}+3 X_{2} \leq 165
$$

$$
x_{1}, x_{2} \geq 0
$$

Q. 2
(a) What is Transportation Problem ? Also derive the mathematical formulation of Transportation Problem.
(b) Solve the following minimal assignment problem.

| Man |  | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | 8 | 4 | 2 | 6 | 1 |
|  | B | 0 | 9 | 5 | 5 | 4 |
|  | C | 3 | 8 | 9 | 2 | 6 |
|  | D | 4 | 3 | 1 | 0 | 3 |
|  | E | 9 | 5 | 8 | 9 | 5 |

(c) Solve the following Transportation Problem Matrix Minima method.

|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | Supply |
| :---: | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{O}_{1}$ | 42 | 48 | 38 | 37 | 140 |
| $\mathrm{O}_{2}$ | 40 | 49 | 52 | 51 | 130 |
| $\mathrm{O}_{3}$ | 39 | 38 | 40 | 43 | 170 |
| Demand | 80 | 90 | 110 | 160 |  |

OR
Q. 2
(a) Solve the following Transportation Problem by VAM method.

|  | I | II | III | IV | $a_{j}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| A | 11 | 13 | 17 | 14 | 250 |
| B | 16 | 18 | 14 | 10 | 300 |
| C | 21 | 24 | 13 | 10 | 400 |
| b $_{j}$ | 200 | 225 | 275 | 250 |  |

(b) Solve the following Transportation Problem by North West corner method.

|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ | $\mathrm{D}_{4}$ | $\mathrm{D}_{5}$ | Supply |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{O}_{1}$ | 4 | 5 | 7 | 9 | 10 | 20 |
| $\mathrm{O}_{2}$ | 3 | 1 | 2 | 6 | 9 | 30 |
| $\mathrm{O}_{3}$ | 8 | 12 | 15 | 30 | 4 | 17 |
| $\mathrm{O}_{4}$ | 3 | 2 | 10 | 13 | 17 | 13 |
| Demand | 40 | 8 | 7 | 19 | 6 | 80 |

(c) Solve the following minimal assignment problem.

Job

|  |  | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | 7 | 9 | 3 | 3 | 2 |
|  | B | 6 | 1 | 6 | 6 | 5 |
| Man | C | 3 | 4 | 9 | 10 | 7 |
|  | D | 1 | 5 | 2 | 2 | 4 |
|  | E | 6 | 6 | 9 | 4 | 2 |

Q. 3
(a) What are the limitations of Game theory?
(b) Solve the following game using Graphical method.

Player B

|  |  | I | II | III | IV |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Player A | I | 2 | 2 | 3 | -1 |
|  | II | 4 | 3 | 2 | 6 |

(c) Solve the following game using dominance principle.

|  |  | I | II | III | IV |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Player A | I | 3 | 5 | 9 | 6 |
|  | II | 5 | 6 | 7 | 8 |
|  | III | 8 | 7 | 8 | 7 |
|  | IV | 4 | 2 | 5 | 3 |

OR
Q. 3
(a) Explain types of Game.
(b) Solve the following game using dominance principle.

Player B

Player A

|  | I | II | III | IV |
| :--- | :--- | :--- | :--- | :--- |
| I | 3 | 2 | 4 | 0 |
| II | 3 | 4 | 2 | 4 |
| III | 4 | 2 | 4 | 0 |
| IV | 0 | 4 | 0 | 8 |

(c) Solve the following game graphically whose payoff matrix for the Player $A$ is

|  |  | Player B |  |
| :--- | :--- | :--- | :--- |
|  |  | I | II |
| Player A | I | 2 | 4 |
|  | II | 2 | 3 |
|  | III | 3 | 2 |
|  | IV | -2 | 6 |

Q. 4
(a) Write a note on variations due to assignable causes.
(b) Draw $\bar{X}$ and $R$ charts for the following data and state your conclusions.

| Sample <br> No. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\overline{\mathrm{X}}$ | 12.8 | 13.1 | 13.5 | 12.9 | 13.2 | 14.1 | 12.1 | 15.5 | 13.9 | 14.2 |
| R | 2.1 | 3.1 | 3.9 | 2.1 | 1.9 | 3.0 | 2.5 | 2.8 | 2.5 | 2.0 |

## OR

## Q. 4

(a) Write the difference between Variable charts and Attribute charts.
(b) The number of defects noticed in 20 clothes are given below. 05
$1,4,3,2,5,4,6,7,2,3,2,5,7,6,4,5,2,1,3,8$.
Decide whether the process is in a state of statistical control or not?
(c) Samples of 400 bottles were taken daily for 15 days from a pharmaceutical 05 company. The number of defective seals in these bottles are given below.
Draw P chart for the data.
Draw $P$ chart for the data .

| Date | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 15 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Defective <br> seals | 28 | 18 | 40 | 42 | 32 | 62 | 50 | 10 | 30 | 22 | 80 | 62 | 76 | 56 |

